

**2007 Hoover HS Math Tournament  
Pre-Algebra Written Test**

1. Evaluate:  $3^2 + 3(2 - 3) + 2^3$ 
  - a) 14
  - b) 12
  - c) 8
  - d) -4
  - e)NOTA
2. Write  $.0\overline{7}$  as a fraction in lowest terms.
  - a)  $\frac{7}{10}$
  - b)  $\frac{7}{90}$
  - c)  $\frac{7}{99}$
  - d)  $\frac{77}{99}$
  - e)NOTA
3. Find the probability of choosing a number R from the set  $R = \{0,1,2,3,4,5,6,7,8,9\}$  such that  $32,3R4$  is divisible by 6.
  - a)  $\frac{4}{5}$
  - b)  $\frac{2}{5}$
  - c)  $\frac{3}{5}$
  - d)  $\frac{1}{10}$
  - e)NOTA
4. If  $a - b = 6$  and  $ax + 2x - bx = 16$ , find x.
  - a) 6
  - b) 12
  - c) 2
  - d) 8
  - e)NOTA
5. Find x  $(4^x)(64)(8) = 2^8$ 
  - a) 1
  - b)  $\frac{1}{2}$
  - c)  $-\frac{1}{2}$
  - d) 2
  - e)NOTA
6. How many times does the graph of the function  $y = x^2 - 6$  cross the x-axis?
  - a) 6
  - b) 1
  - c) 2
  - d) 0
  - e)NOTA
7. What is the probability that the total obtained after rolling a pair of dice is a non-prime number?
  - a)  $\frac{1}{2}$
  - b)  $\frac{11}{18}$
  - c)  $\frac{5}{12}$
  - d)  $\frac{7}{12}$
  - e)NOTA
8. According to the journal of pediatric medicine, a child's weight should increase by 10% each month. If a child has a current weight of 6 lbs. 4 oz., how much will she weigh in 2 months?
  - a) 7 lbs. 6oz.
  - b) 7 lbs. 9oz.
  - c) 7 lbs. 8oz.
  - d) 120 lbs.
  - e)NOTA
9. A class of junior high mathematicians developed a new way to measure angles called slices. The sum of the angles of a scalene right triangle is 200 slices. The sum of the angles of a pentagon equals \_\_\_\_\_ slices.
  - a) 400
  - b) 360
  - c) 540
  - d) 600
  - e)NOTA
10. If  $A = B+1$  and  $B=2C+2$  and  $C = 3A+3$  find A.
  - a)  $-\frac{9}{5}$
  - b) 2
  - c)  $-\frac{1}{2}$
  - d) 6
  - e)NOTA
11. Farmer Ted walks 50 yards around the circumference of his circular field. If this is  $\frac{1}{10}$  of the total circumference, what is the area of his field?
  - a)  $\frac{10}{\pi}$
  - b)  $\frac{500}{\pi}$
  - c)  $2500\pi$
  - d)  $\frac{62500}{\pi}$
  - e)NOTA

12. A circle is placed perfectly inside a square. Find the ratio of the area of the shaded region to the area of the un-shaded region.



- a)  $\frac{4-\pi}{\pi}$       b)  $\frac{1}{\pi}$       c)  $\frac{4}{\pi}$       d)  $\frac{\pi}{2\pi-1}$       e)NOTA

13. If point A ( 2 , 5 ) is rotated  $90^\circ$  ccw about the origin and then reflected across the line  $y=x$ , which quadrant will the resulting point be in?

- a) I      b) II      c) III      d) IV      e)NOTA

14. What is the sum of the numbers in the 5<sup>th</sup> row of Pascal's triangle?

- a) 5      b) 10      c) 16      d) 32      e)NOTA

15. At which of the following times is the obtuse angle formed by the hour and minute hand of a clock equal to  $105^\circ$ ?

- a) 4:00      b) 1:30      c) 9:30      d) 10:15      e)NOTA

16. The price of an item is reduced by  $\frac{1}{4}$  and then by  $55\frac{5}{9}\%$ . What would the total percent decrease in price be?

- a) 74 %      b)  $66\frac{2}{3}$  %      c)  $33\frac{1}{3}$  %      d) 86.1 %      e)NOTA

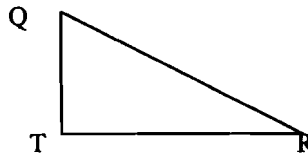
17. Find the area of the region bounded by the graphs of  $y > 0$ ,  $x > 0$ , and  $y < -\frac{1}{2}x + 8$ .

- a) 32 units<sup>2</sup>      b) 64 units<sup>2</sup>      c) 128 units<sup>2</sup>      d) 16 units<sup>2</sup>      e)NOTA

18. Jack and Jill leave the same hill at the same time. Jack heads due north at 3 mph. Jill heads due east at 4 mph. How many hours does it take for them to be 20 miles from each other?

- a) 3.5 hrs.      b) 4 hrs.      c) 2 hrs.      d) 3 hrs.      e)NOTA

19. If  $\sin Q = \frac{TR}{QR}$  and  $\cos Q = \frac{QT}{QR}$  Find:  $\frac{\sin Q}{\cos Q}$



- a) 1      b)  $\frac{QR}{QT}$       c)  $\frac{TR}{QT}$       d)  $\frac{QT}{TR}$       e)NOTA

20. The mean of  $\frac{2}{3}$ ,  $\frac{3}{4}$ , and  $\frac{x}{5}$  is  $\frac{41}{36}$ . Find x.

- a) 18      b) 6      c) 60      d) 10      e)NOTA

21. The number halfway between  $\frac{2}{3}$  and  $\frac{12}{9}$  is:

- a) 1      b)  $\frac{7}{6}$       c)  $1\frac{1}{2}$       d)  $\frac{7}{12}$       e)NOTA

22. A 40 inch diameter tire with a width of 6 in. is rolled up against a  $90^\circ$  corner. Find the volume of the space formed by the tire and the corner.

- a)  $400\pi \text{ in.}^3$       b)  $1800\pi \text{ in.}^3$       c)  $400 - 100\pi \text{ in.}^3$       d)  $2400 - 600\pi \text{ in.}^3$       e) NOTA

23. If  $x$  and  $y$  are both integers with  $x > 0$  and  $y < 0$ , which of the following must always be true?

- a)  $xy > 0$       b)  $x + y < 0$       c)  $x - y > 0$       d)  $x - y < 0$       e) NOTA

24. A bug on a road is squashed by a rolling car tire. If the bug is now stuck to the 30 inch diameter tire, how far is the bug from its original position after  $2\frac{1}{2}$  revolutions?

- a)  $15\sqrt{4 + 25\pi^2} \text{ in.}$       b)  $30\sqrt{1 + \pi^2} \text{ in.}$       c)  $30\pi\sqrt{2} \text{ in.}$       d)  $15\sqrt{1 + 4\pi} \text{ in.}$       e) NOTA

25. A circle with a radius of 5 units has a center  $P(3, 4)$ . Find the coordinate on the circle that is farthest from the origin.

- a)  $(8, 6)$       b)  $(6, 8)$       c)  $(7, 12)$       d)  $(10, 0)$       e) NOTA

TB1 Find all answers for  $r$ :  $3r(4 - r) - 3r(r - 4) = 3r$

TB2 Evaluate  $(3.2 \times 10^5 + 4.4 \times 10^4)^2$ . Write answer in scientific notation.

TB3 Find the last 2 digits of  $5^{347}$