7th Grade Ciphering - Hoover High School Math Tournament - February 22, 2003

- 1-1. Find the midpoint of the two points (2, 5) and (-1, -3). Ans: $\left(\frac{1}{2}, 1\right)$
- 1-2 In an election, nine-sixteenths of voters voted "NO", while the other 98 voted "YES". How many people voted?

1-3.
$$123_4 = 8$$
 Ans: 33_8

1.4. Given:
$$a\#b = \frac{a^2 + b^2}{ab}$$
. Evaluate: $(3\#4) + (8\#3)$ Ans: $\frac{41}{8}$

- 1-5. What is 17 % of 300? Ans: 51
- 2-1. In the pattern 5,-10,-12, _____, 22,-44,-46,92,90, what is the missing term?

- 2-2. Three fair dice are rolled. What is the probability that the sum of the numbers is 17?

 Ans: $\frac{1}{72}$
- 2-3. Evil Genius Bob can paint a castle in 6 hours. His assistant Roger can paint a castle in 10 hours. How many hours will it take them to paint a castle together?

 Ans: $\frac{15}{4}$
- 2-4. For the set of numbers $\{10, 8, 0, 6, 6\}$, x = mean, y = median, and z = mode. Find $z + \frac{y}{x}$.
- 2-5. Find the distance between the points (3,7) and (-1,4)? Ans: 5
- 3-1. Jill is 6 years older than Emily. Eight years ago Jill was two times as old as Emily was then. How old will Jill be in four years?

 Ans: 24
- 3-2. A flying monkey is tied to the top of a 12 foot pole by a 3 foot long rope. What is the volume of the sphere in which the monkey can fly? Ignore the volume of the pole.

 Ans: 36π cubic feet

3-3. Simplify:
$$\frac{\left(\frac{\frac{1}{2} + \frac{2}{3} \times \frac{3}{4} + \frac{4}{5}}{\frac{6}{5}}\right) - 1}{4}$$

Ans:
$$\frac{1}{8}$$

3-4. The points (-3,3), (-3,-2), (4,-2) form a triangle. Find the area of this triangle.

Ans:
$$\frac{35}{2}$$
 or 17.5

3-5 Evaluate, writing your answer in scientific notation, $(1.609 \times 10^{-19}) \times 2000$

Ans:
$$3.218 \times 10^{-16}$$

4-1. Solve for $x: \frac{7x}{2} - 7 = 21$

4-2. Bob has a rectangular prism shaped tank with dimensions $14 \times 6 \times 5$. How many monkeys can he place in the tank if each monkey needs 5 cubic units of space?

- 4-3. If the area of a circle is 256π , what is the circumference of the circle? Ans: 32π
- 4-4. Simplify:

$$5+3\left[(32-28)(3\times9\div28)^{\left[\left[(16-2\times4)\div8\right]-1\right]}\right]$$

- 4-5 In a monkey race, Michael the Monkey can complete a 1.5 mile race in 10 minutes. How fast can Michael the Monkey run in miles per hour?

 Ans: 9 mph
- E-1. Given: 2x+5y=16 and x+3y=5. Find: x-y. Ans: 29
- E-2. Erin has a closed box that is a rectangular prism. What is the surface area of the box if its dimensions are $14 \times 6 \times 5$?

 Ans: 368
- E-3 A circular rug with a diameter of 6 meters is on a rectangular floor that measures 20 meters by 6 meters. What is the area of the floor that is not covered by the rug?

 Ans: $120-9\pi$